



Reg. No. :

Name :

First Semester M.Tech. Degree Examination, February 2015
(2013 Scheme)
Electronics and Communication
Stream : Signal Processing
TSC 1004 : MULTIRATE SYSTEM AND WAVELETS

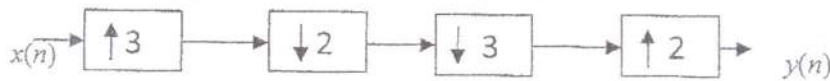
Time : 3 Hours

Max. Marks : 60

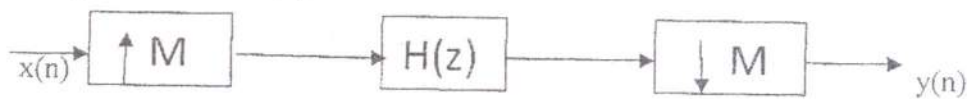
Instruction : Answer any two questions from each Module.

Module – I

1. a) Derive the relation between input and output spectra for an M-fold decimator. Illustrate with an example. 5
- b) For the system shown in the Fig. below, find simplified expression for $y(n)$ in terms of $x(n)$. 5



2. a) Derive output $Y(z)$ of the system shown below in terms of the polyphase components of $H(z)$. 5



- b) Develop a two band polyphase decomposition of the following transfer function 5

$$\frac{2 + 3.1z^{-1} + 1.5z^{-2}}{1 + 0.9z^{-1} + 0.8z^{-2}}$$

3. What is the necessary and sufficient condition for perfect reconstruction ? Show that M-channel uniform DFT filter bank is a perfect reconstruction system. Also find the synthesis filters in the DFT filter bank. 10



P.T.O.



Module – II

4. Given $\Psi(t) = \begin{cases} 1, & 0 \leq t < \frac{1}{2} \\ -1, & \frac{1}{2} \leq t < 1 \\ 0 & \text{otherwise} \end{cases}$ and $\psi_{m,n}(t) = 2^{-m/2} \Psi(2^{-m} t - n), m, n \in \mathbb{Z}$. 10

Prove that the set of functions $\{\psi_{m,n}(t)\}_{m,n \in \mathbb{Z}}$ forms an orthogonal basis for $L_2(\mathbb{R})$.

5. Describe the necessary conditions to be considered for deriving orthogonal wavelet system coefficients. 10
6. Describe digital filter implementation of Haar wavelet decomposition. 10

Module – III

7. Give the advantages of biorthogonal wavelet system over orthogonal system. Also explain signal representation using biorthogonal wavelet system. 10
 8. Derive Daubechies wavelet system with three vanishing moment (a 6-tap wavelet system) using frequency domain approach. 10
 9. Explain in details the application of wavelets in denoising. 10
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