



Reg. No. :

Name :

First Semester M.Tech. Degree Examination, March 2013
(2008 Scheme)

TMC - 1001 - ADVANCED DIGITAL SIGNAL PROCESSING

Time : 3 Hours

Max. Marks : 100

- Instructions :** 1) Answer any five.
2) All questions carry equal marks.

1. a) The signal $x(n]$ is defined by

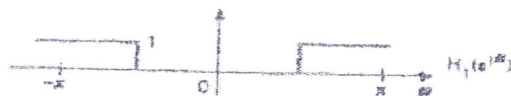
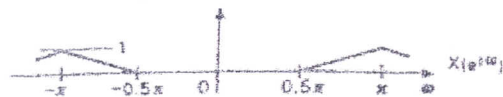
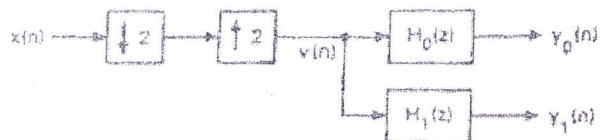
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$$x(n) = a^n \quad n > 0$$

$$= 0 \quad \text{otherwise}$$

- i) Write the expression and plot the signal, if $x(n]$ is decimated with a factor of three.
- ii) Write the expression and plot the signal, if $x(n]$ is interpolated with a factor of three.

b) Consider the structure shown below with input transforms and filter responses as indicated. Sketch the quantities $Y_0(e^{j\omega})$ and $Y_1(e^{j\omega})$ and interpret.

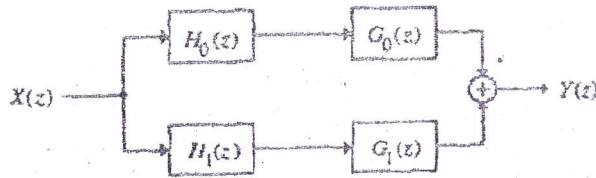


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P.T.O.



2. a) Explain a 2 channel QMF bank. What are the distortions present ? How is perfect reconstruction achieved ? 10
- b) Let $H_0(z) = (1+z^{-1})/2$ and $H_1(z) = (1-z^{-1})/2$. Determine the synthesis filters $G_0(z)$ and $G_1(z)$ so that the structure shown below is a perfect reconstruction filter bank. 10



3. a) Discuss causality issue of a decimator. 6
- b) Obtain 2 band polyphase decomposition of the transfer function given below : $H(z) = (1-5z^{-1})/(1+3z^{-1})$. 6
- c) Let $H(z)$ represents an FIR filter of length 8 with impulse response coefficients $h(n) = (0.3)^n$ for $0 \leq n \leq 7$ and zero otherwise. Find the poly phase components $E_0(z)$ and $E_1(z)$. 8
4. a) Basis sets of scaling functions span a nested space. State your comments on the above statement. 6
- b) A signal in V_1 space is designated as follows : $[4, 2, 6, -2, 4, 6, 2, 2]$. Perform Haar decomposition into V_0 and W_0 spaces. 8
- c) State uncertainty principle and discuss its significance using time frequency tiling. 6
5. a) State the relationship between different function spaces in a biorthogonal wavelet system. What is the motivation for designing biorthogonal systems ? 5
- b) Project the function $f(x) = x$ onto the space spanned by $\phi(x), \psi(x), \psi(2x), \psi(2x-1) \in L^2[0,1]$ where
- $$\phi(x) = \begin{cases} 1, & 0 \leq x \leq 1/2 \\ 0, & \text{otherwise} \end{cases}$$
- $$\psi(x) = \begin{cases} 1, & 0 \leq x \leq 1/2 \\ -1, & 1/2 \leq x \leq 1 \\ 0, & \text{otherwise} \end{cases}$$
- Sketch the projection of $f(x)$ to this space. 15
6. What is the basic concept of linear prediction analysis ? Explain Levinson-Durbin algorithm. 20